quent than from the external callus. Most shoots arose from external callus produced by the pith and by the phloem, though in some cases the xvlem and endodermis also were involved to a small extent. These regenerated shoots always established organic union with the vascular tissue of the decapitated shoot and became functional.

This observation of shoot regeneration by cabbage following treatment with Beta (3) indole-acetic acid is not an instance of induction of a new characteristic by a chemical agent. Occasionally (very rarely) decapitated control cabbage plants produced shoots without application of the acid. The chemical treatment apparently merely induces the internal conditions requisite for expression of a capacity which normally rarely comes to expression in the cabbage plant.

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## EXACT PROBABILITIES IN CARD-MATCHING PROBLEMS

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A DECK of mn playing-cards composed of m suits of n cards each, may be arranged in  $(mn)!/(n!)^m$  ways. If one of these is compared with some standard order, the number of coincidences is called the score. The frequency of any score r may be denoted by (r; m,n). Huntington<sup>1</sup> gave the values of (r; 3,3) and (r; 4,4). He considered the labor in the determination of (r;

TABLE 1

6×6									
Score	Frequency								
$\begin{array}{c} 0 & \dots \\ 1 & \dots \\ 2 & \dots \\ 3 & \dots \\ 4 & \dots \\ 5 & \dots \\ 5 & \dots \\ 6 & \dots \\ 7 & \dots \\ 8 & \dots \\ 9 & \dots \\ 11 & \dots \\ 12 & \dots \\ 11 & \dots \\ 12 & \dots \\ 13 & \dots \\ 14 & \dots \\ 13 & \dots \\ 14 & \dots \\ 15 & \dots \\ 15 & \dots \\ 16 & \dots \\ 17 & \dots \\ 18 & \dots \\ 19 & \dots \\ 21 & \dots \\ 22 & \dots \\ 23 & \dots \\ 24 & \dots \\ 22 & \dots \\ 23 & \dots \\ 24 & \dots \\ 25 & \dots \\ 26 & \dots \\ 27 & \dots \\ 27 & \dots \\ 28 & \dots \\ 28 & \dots \\ 29 & \dots \\ 29 & \dots \\ 20 & \dots \\ 21 & \dots \\ 21 & \dots \\ 21 & \dots \\ 22 & \dots \\ 22 & \dots \\ 23 & \dots \\ 24 & \dots \\ 25 & \dots \\ 26 & \dots \\ 27 & \dots \\ 27 & \dots \\ 28 & \dots \\ 28 & \dots \\ 31 & \dots \\ 33 & \dots \\ 33 & \dots \\ 34 & \dots \\ 35 & \dots \\ 36 & \dots \end{array}$		$\begin{array}{c} 4\\ 28\\ 98\\ 8355\\ 450\\ 462\\ 289\\ 182\\ 200\\ 48\\ 200\\ 7\\ 2\end{array}$	$165 \\ 996 \\ 864 \\ 341 \\ 1123 \\ 793 \\ 524 \\ 575 \\ 980 \\ 735 \\ 584 \\ 2334 \\ 58 \\ 2334 \\ 2$	949 446 744 808 281 967 784 670 943 9943 9943 995 4656 8545 6566 8844 038 8545 813 313 734 855 13 313 1	$\begin{array}{c} 769\\ 742\\ 213\\ 829\\ 078\\ 827\\ 435\\ 735\\ 100\\ 735\\ 735\\ 100\\ 371\\ 196\\ 462\\ 27\\ 372\\ 872\\ 804\\ 225\\ 804\\ 225\\ 22\\ 2\\ 2\end{array}$	$\begin{array}{c} 769\\ 915\\ 619\\ 962\\ 568\\ 100\\ 823\\ 001\\ 530\\ 001\\ 823\\ 001\\ 163\\ 801\\ 3729\\ 954\\ 801\\ 3729\\ 584\\ 448\\ 807\\ 584\\ 448\\ 897\\ 5560\\ 230\\ 811\\ 1\end{array}$	$\begin{array}{c} 961\\ 700\\ 952\\ 293\\ 422\\ 016\\ 073\\ 786\\ 005\\ 140\\ 005\\ 220\\ 448\\ 874\\ 642\\ 222\\ 498\\ 874\\ 4642\\ 272\\ 755\\ 212\\ 404\\ 404\\ 852\\ 498\\ 852\\ 498\\ 852\\ 498\\ 852\\ 445\\ 488\\ 852\\ 445\\ 445\\ 852\\ 445\\ 852\\ 445\\ 852\\ 445\\ 852\\ 445\\ 852\\ 445\\ 852\\ 445\\ 852\\ 852\\ 445\\ 852\\ 852\\ 852\\ 852\\ 852\\ 852\\ 852\\ 85$	828 420 591 367 086 912 332 052 868 868 230 505 505 505 505 793 0394 992 240 352 240 352 240 352 240 352 243 318 8661 048 57 7703 877 709 865 314 316 772 338 421 357 243 877 887 887 877 877 877 877 877 877 87	$\begin{array}{r} 425\\ 640\\ 7000\\ 200\\ 175\\ 160\\ 336\\ 640\\ 500\\ 504\\ 850\\ 400\\ 520\\ 400\\ 520\\ 400\\ 520\\ 400\\ 520\\ 400\\ 600\\ 850\\ 600\\ 800\\ 400\\ 800\\ 400\\ 800\\ 400\\ 800\\ 400\\ 800\\ 8$
	2	670	177	736	637	<b>149</b>	247	308	800

5.5) to be prohibitive. Sterne<sup>2</sup> found the values of (21; 5,5) up to (25; 5,5) but knew of no way to determine these for smaller r. Greville<sup>3</sup> has recently found all values of (r; 5,5); his solutions are correct, but involve much labor.

The problem is by no means as difficult as these papers imply. Macmahon<sup>4</sup> gave a direct method of attack by which Greville's results may be checked with about 12 hours of machine calculation. I have recently determined the values of (r; m,n) for all m and n less than 7 (m and n not being necessarily equal). The frequencies for the case in which both m and n are 6 are given in Table 1.

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<sup>1</sup> Huntington, SCIENCE, 86: 499-500.

- <sup>2</sup> Sterne, SCIENCE, 86: 500-501.
- <sup>3</sup> Greville, Journal of Parapsychology, March, 1938.

4 Macmahon, Combinatory Analysis, Vol. 1, p. 99-112, Cambridge, 1915.

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