

Geophysicists Ponder Hints Of Otherworldly Water

SAN FRANCISCO—More than 7000 geophysicists gathered here from 8 to 12 December for the annual fall meeting of the American Geophysical Union (AGU). All eyes were on a session addressing the claim that tiny comets pummel Earth every minute, but more distant wonders—oceans within Jupiter's moons—were one topic in a little-noticed Friday afternoon session.

Tidings of a Hidden Ocean?

Looking at the tortured, icy surface of Jupiter's moon Europa, it's easy to imagine a liquid ocean stirring below it. Indeed, planetary geologists observing the fractures and disruption of the crust—features also seen in the ice pack of our Arctic Ocean—have argued that an ocean, one that could be teeming with life, lies just a few kilometers down (*Science*, 19 December 1997, p. 2041). But the geological arguments aren't absolutely convincing; they don't rule out the possibility that the moon once had an ocean that has long since frozen solid. Now an unexpected new clue to an ocean on Europa—as liquid and briny as our own—has emerged.

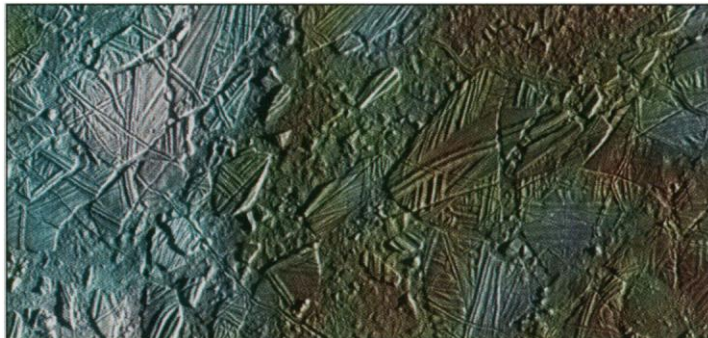
Looping past the satellite, the Galileo spacecraft has picked up what may be traces of a magnetic field induced in a subsurface ocean by Jupiter's own powerful field. The evidence is not yet conclusive, but if further close flybys bear it out, "it would be the strongest evidence so far for an ocean," says planetary physicist David Stevenson of the California Institute of Technology. And Europa may not be unique. In a surprising twist, the same kinds of clues are also hinting at an ocean in another jovian moon, Callisto.

Soon after Galileo began inspecting Jupiter's four major satellites in December 1996, it picked up unexpected magnetic signatures near these bodies. Ganymede had an unmistakable magnetic field, generated in the same way as Earth's: by the churning of a liquid metal core. But the fields Galileo detected near Io, Europa, and Callisto were much weaker. Instead of originating within the moons, researchers speculated, these weak magnetic signatures could result from plasmas of charged particles swirling nearby.

Then two researchers, Stevenson and planetary magnetist Fritz Neubauer of the University of Köln in Germany, independently began thinking of other ways to explain the weak fields Galileo had detected. Both hit on the

idea that they might be induced within a satellite by Jupiter's own magnetic field. For example, Stevenson reasoned that if Europa did have an ocean 10 to 100 kilometers beneath its surface ice, the jovian magnetic field would be sweeping through the water constantly because the tilted field wobbles like a tipsy top as the planet rotates. If the ocean were salty enough, and thus a good electrical conductor, the moving field would induce electrical currents—called eddy currents—in the ocean. These currents would in turn create a magnetic field oriented roughly opposite to Jupiter's.

At the AGU meeting, Lee Bennett, Margaret Kivelson, and Krishan Khurana of the Uni-



An ice-encrusted ocean? This color-enhanced image of Europa dramatizes the surface disruption, suggesting that an ocean lies below.

versity of California, Los Angeles (UCLA), reported what Kivelson called a "rather impressive" fit between Stevenson's calculated field and the observations. Galileo's first magnetic field data from near Europa showed that the field at the spacecraft waxed and waned during the flyby much as Stevenson had predicted for an induced field. "I was shocked and pleased," says Kivelson, who is the principal investigator of the Galileo magnetometer. "It was the first time it began to make sense." A second Europa pass recorded a magnetic signature that was much more variable, but still roughly consistent with an induced field, says Stevenson.

The UCLA group then applied Stevenson's model to Callisto. Galileo gravity data had initially seemed to imply that Callisto is nothing but a mix of rock and ice. Neubauer suggested, however, that the magnetic signature Galileo picked up looked much like an induced field.

He was right. "The astonishing thing is that the model works even better for Callisto" than for Europa, says Stevenson—suggesting that Callisto has a salty ocean 200 kilometers down. According to geophysicist Gerald Schubert of UCLA and his Galileo colleagues, the gravity data don't rule out such an ocean after all. Their revised interpretation, reported at the meeting, calls for an outer shell of water that could be frozen on the outside but liquid inside.

More flybys during Galileo's 2-year "extended" mission, which began in December, could firm up the case for one or both of these oceans. Stevenson remains cautious, however. "I still wonder whether there's some way external to the satellite to produce this effect," he says. "We have a poor enough understanding of the plasmas around these bodies that maybe we're missing something."

'Atmospheric Holes' Assailed

The idea that house-sized comets are pelting the Earth 25,000 times a day appears just as implausible now as it did when space physicist Louis Frank of the University of Iowa in Iowa City first proposed it in 1986. But the dark spots seen in satellite images of the upper atmosphere, which Frank had identified as "atmospheric holes"—the watery traces of his comets—have come back to tease space scientists. Dismissed as instrument noise 10 years ago, the spots reappeared last year in images from a new satellite, Polar, persuading a few researchers that something peculiar—although not a rain of small comets—is going on in the upper atmosphere (*Science*, 30 May 1997, p. 1333). Frank and his critics are now deadlocked about whether the spots are real, and they battled at a packed session of the meeting.

Frank's claim had seemed stronger last year because he said that the spots appeared not only in his own camera aboard Polar, but also in the Ultra-Violet Imager (UVI) of one of his colleagues on the Polar team, George Parks of the University of Washington, Seattle. Frank also cited the "smearing" of some spots as evidence that they were real, saying it resulted from the Polar spacecraft's unintended wobble.

But Parks had his name removed from the paper claiming a two-camera detection, and his own analysis of spots in his UVI images, which he first took public a month and a half ago, suggested that the spots behave just like artifacts somehow produced inside the camera. (See *Science*, 14 November 1997, p. 1217; the results also appeared in the 15 December issue of *Geophysical Research Letters*.) He found, for example, that the number of spots of a given size decreased steadily from the smallest to the largest, just like the noise in lab

MATHEMATICS

Sieving Prime Numbers From Thin Ore

calibration images. And instead of being smeared into two spots along the direction of the Polar spacecraft's wobble, as Frank had claimed, closely spaced spots in UVI images fell in random directions from each other.

Parks has now repeated the same type of analysis on spots from Frank's visible-light imager and reports finding the same noiselike behavior. The spots are "internal to the camera," he said at the meeting. "There's no evidence anything is coming from the outside."

Frank responded that Parks is analyzing the wrong spots. All but the largest dark spots are instrument noise, Frank said, adding, "There's no reason to include these enormous amounts of noise. You have to do something else to the data." If the spots are indeed clouds of water from incoming small comets, he reasoned, a cloud's motion across the field of view should add a third spot to the two created by the wobble motion of the spacecraft. Five of the candidate atmospheric holes in Parks's UVI images, said Frank, have three spots in the triangular orientation predicted by Polar's wobble. "I don't see how you can miss that sort of thing," said Frank.

Frank also looked at whether the spots shrink and disappear when Polar's eccentric orbit carries it farther above the atmosphere, as they should if they are real. Eighty percent of the large dark spots that Frank thinks are real holes disappeared between altitudes of around 25,000 kilometers and 41,000 kilometers, he said. "There's nothing you can do about this," said Frank. "It's the ultimate test. The holes are a geophysical phenomenon."

Parks, among many others, remained unconvinced. He notes that if the holes are real, then the three spots each one produces should be connected by slightly darkened streaks where the image was smeared across the detectors, but the three spots in the example he saw Frank present actually had slightly brighter spaces between them. And although Parks has not yet checked the altitude dependence of spots, he notes that Bruce Cragin of CES Network Services in Farmers Branch, Texas, and his colleagues did apply the altitude test in 1987 to spots in images from the Dynamics Explorer spacecraft, in which Frank first discovered atmospheric holes. When spacecraft altitude varied by a factor of 3, the abundance as well as the size of spots remained the same.

"I don't think the San Francisco exercise has changed many minds," says planetary scientist Thomas Donahue of the University of Michigan, Ann Arbor, who has leaned toward accepting the atmospheric holes as real. But some minds could change after other researchers get their shot at the data. NASA is expected to fund more analyses this year, and Frank plans to release all his Polar data on CD-ROMs this month, so that other space scientists can see—or fail to see—the spots for themselves.

—Richard A. Kerr

Mathematicians have known since Euclid that there is an infinite number of prime numbers. For the last 100 years, they have even had a good way to determine, approximately, how many primes there are up to any given number. But the finer points of how primes are distributed remain, by and large, mysterious. In particular, mathematicians are almost always unable to take an infinite but sparsely distributed set of integers, such as the values of $n^2 + 1$, and tell how rich in primes it is.

That barrier is beginning to yield. In what number theorists are calling a major breakthrough, two mathematicians have developed powerful new techniques for assaying such "thin" subsets of integers for primes. As John Friedlander of the University of Toronto and Henryk Iwaniec of Rutgers University in New Brunswick, New Jersey, report in a paper to appear in the *Annals of Mathematics*, they have refined a tool known as the asymptotic sieve, developed in the 1970s by Enrico Bombieri of the Institute for Advanced Study in Princeton, New Jersey. Their first conquest: a remarkably thin sequence consisting of numbers of the form $a^2 + b^4$. Friedlander and Iwaniec's new sieve shows that even though most such numbers are composite—products of prime factors—the sequence includes an infinite number of primes.

"This is totally new," says Bombieri. The conclusion, he adds, "is what you would expect from heuristic arguments, but to prove things is another matter!" In his opinion, Friedlander and Iwaniec have written "one of the most important papers in analytic number theory of the century." It "will find a lot of applications" in exploring the distribution of primes.

Roughly speaking, a mathematical sieve determines the abundance of primes in a long list of numbers by estimating how many numbers remain when multiples of small primes are removed—a procedure that sifts out most composite numbers. For example, of the numbers between 169 and 289 (the squares of the primes 13 and 17), roughly half remain when you delete the even numbers, two-thirds of those remain after the multiples of 3 are removed, etc. Sieving the 120 numbers in the sequence yields an estimate of $120 \times (1/2) \times (2/3) \times (4/5) \times (6/7) \times (10/11) \times (12/13) = 23$ primes. That's

close to the exact count, 22. Similar sieves can be designed for other number sequences. The real work comes in analyzing the errors in such estimates to get rigorous results.

The errors are easiest to estimate for "dense" sequences such as 1, 5, 9, 13, etc.—a progression that contains roughly one-fourth of all numbers up to a given size. But Friedlander and Iwaniec's sequence contains a vanishingly small fraction of the integers. That thinness makes it impossible to estimate the errors in the usual way, putting the sequence out of the reach of previous sieves. "Nobody dreamed you could analyze such sequences," says Bombieri.

The new techniques rely on special algebraic properties of the formula

$a^2 + b^4$. In a number system

known as the Gaussian integers, which enlarges the set of ordinary integers by including i , the square root of -1 , such numbers can always be factored as $(a + b^2i)(a - b^2i)$. By putting their numbers into this form, Friedlander and Iwaniec were able to exploit the well-developed theory of algebraic numbers to get a handle on the errors when they applied their sieve.

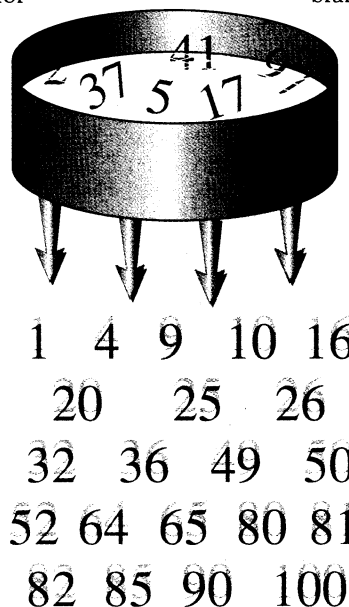
The combination of algebraic number theory and sieve techniques is what Peter Sarnak of Princeton University finds most impressive.

"These are two different worlds, algebra and the

sieve," he notes. But because the technique relies on properties found in only a small fraction of sequences, many of sieve theory's dearest problems still look hopeless. In particular, numbers of the form $n^2 + 1$ —1, 2, 5, 10, 17, 26, etc.—almost certainly include an infinite number of primes; indeed, number theorists have even conjectured an estimate for how many there are up to any given integer in the sequence. But no proof appears to be forthcoming. Number theorists are also convinced that each interval between consecutive squares contains at least one prime, but have no idea how to prove it.

"The answer to most of these questions is, we don't know," says Andrew Granville, a number theorist at the University of Georgia in Athens. "It's frightening how pathetic our knowledge is!"

—Barry Cipra



Prime cut. The sieve captures the primes in the sequence of numbers of the form $a^2 + b^4$, up to 100.

ILLUSTRATION: L. CARROLL