

## The Boranes and Their Relatives

William N. Lipscomb

This year, 1976, the Nobel Prize in Chemistry has been awarded for research in pure inorganic chemistry, in particular, the boranes. May I say that I am most pleased and profoundly grateful. My own orientation to this field has been, as in all of my studies, the relationships of the chemical behavior of molecules to their three-dimensional geometrical and electronic structures. The early work on the molecular structures of boranes by x-ray diffraction led to a reasonable basis for a theory of chemical bonding different from that which is typical in carbon chemistry, and yielded an understanding of the pleasing polyhedral-like nature of these compounds. Assimilated by the preparative chemists, the principles helped to establish a large body of a hitherto unknown chemistry, which made a reality of the expectation that boron, next to carbon in the periodic table, should indeed have a complex chemistry.

In these nearly 30 years, both theoretical and experimental methods have been applied by us and others to areas of inorganic, physical, organic, and biochemistry. For example, these areas include low-temperature x-ray diffraction techniques and the theoretical studies of multicentered chemical bonds including both delocalized and localized molecular orbitals. An early example is extended Hückel theory, originally developed for studies of the boranes, and even now one of the most widely applicable approximate methods for theoretical studies of bonding in complex molecules. More soundly based theories are presently in use by my research students for studying how enzymes catalyze reactions, details of which are based on the three-dimen-

sional structures determined by x-ray diffraction methods. In addition to illuminating particular problems, these developments may contribute toward the redefinition of areas of chemistry and thereby broaden the chemist's view. Our research in the boranes and their related molecular species crosses areas of inorganic, experimental physical, theoretical, and organic chemistry, and includes applications in biochemistry. More simply stated, the area is the study of the relationships of molecular structure to function.

### Boranes and Early Structure Studies

By now, large numbers of polyborane compounds exist: boron hydrides, carboranes, metalloboranes, metallocarboranes, mixed compounds with organic moieties, and others. These discoveries of preparative chemists are relatively recent. Long ago, Alfred Stock established borane chemistry. He developed the experimental techniques that were required for the preparation of the volatile and potentially explosive compounds  $B_2H_6$ ,  $B_4H_{10}$ ,  $B_5H_9$ ,  $B_5H_{11}$ , and  $B_6H_{10}$  and the relatively stable white crystalline  $B_{10}H_{14}$ . This work, beautifully summarized in his Baker Lectures (1), was celebrated at the Third International Meeting on Boron Chemistry this past July in Munich, 100 years after his birth. Sidgwick (2) wrote, "All statements about the hydrides of boron earlier than 1912, when Stock began to work on them, are untrue."

Aside from the classification as either an  $N+4$  or an  $N+6$  series, no simple basis for these unusual formulas was

foreseen before their structures were established. A  $B_6$  octahedron (Fig. 1) was known in certain crystalline borides, and the  $B_{12}$  icosahedron (Fig. 2) was found in boron carbide, but no one realized that a systematic description of the boron arrangements in these hydrides might be based on fragments of these polyhedra. Most electron diffraction work before 1940 supported more open structures, which Pauling (3) described in terms of resonating one-electron bonds. In 1940–1941 Stitt (4) produced infrared and thermodynamic evidence for the bridge structure of  $B_2H_6$  (Fig. 3). More general realization of the correctness of this structure followed the theoretical studies (5, 6), and especially the infrared work of Price (7). The three-center bridge BHB bond was clearly formulated by Longuet-Higgins (6).

The first of the higher hydrides to be characterized structurally was  $B_{10}H_{14}$  (Fig. 4). Kasper, Lucht, and Harker (8) showed that the boron arrangement was a fragment of a  $B_{12}$  icosahedron in which there are four bridge BHB bonds in the open face. Next was  $B_5H_9$  (9) (Fig. 5), a fragment of the  $B_6$  octahedron, and then  $B_4H_{10}$  (10) (Fig. 6), a  $B_4$  unit from these polyhedra. Both of these structures were established by x-ray diffraction in our laboratory, and by electron diffraction at the California Institute of Technology. Our x-ray diffraction results on  $B_5H_{11}$  (11) (Fig. 7) and tetrahedral  $B_4Cl_4$  (12) then set the stage for the beginning of the theory of bonding. The  $B_6H_{10}$  structure (13) (Fig. 8), completing the compounds found by Stock, was to be one of our later x-ray diffraction studies, which were to include many other boranes and related molecules.

It was actually in 1946 that I decided to enter this area of inorganic chemistry. At that time, no reliable methods were gen-

Copyright © 1977 by the Nobel Foundation.

The author is Abbott and James Lawrence Professor of Chemistry, Harvard University, Cambridge, Massachusetts 02138. This article is the lecture he delivered in Stockholm, Sweden, on 11 December 1976 when he received the Nobel Prize in Chemistry. Minor corrections and additions have been made by the author. The article is published here with the permission of the Nobel Foundation and will also be included in the complete volume of *Les Prix Nobel en 1976* as well as in the series Nobel Lectures (in English) published by the Elsevier Publishing Company, Amsterdam and New York.

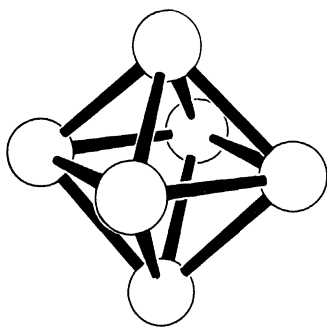
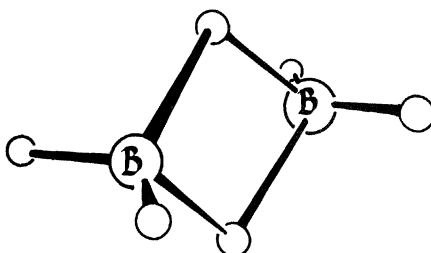
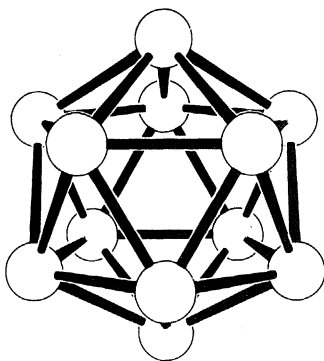


Fig. 1 (top left). The  $B_6$  octahedron, which occurs in certain metal borides, in which each boron atom is bonded externally to a boron atom of another octahedron. In  $B_6H_6^{2-}$  or  $C_2B_4H_6$ , a terminal hydrogen atom is bonded externally to each boron or carbon atom. Fig. 2 (top right). The  $B_{12}$  icosahedron, which occurs in boron carbide  $B_{12}C_3$ , in elementary boron, and in  $B_{12}H_{12}^{2-}$ . The three isomers of  $C_2B_{10}H_{12}$  also have this icosahedral arrangement in which there is one externally bonded hydrogen on each boron or carbon atom. Fig. 3 (bottom right). The geometrical structure of  $B_2H_6$ .



erally available for accumulation of large amounts of x-ray diffraction data at low temperatures. Our methods (14) paralleled those in Fankuchen's laboratory (15) at the then Polytechnic Institute of Brooklyn but were quite independent. Because of the special difficulties of working with the volatile boranes, I chose, among other topics, a series of x-ray diffraction studies of single crystals grown at low temperatures from low-melting liquids for which putative resid-

ual entropy problems existed:  $N_2O_2$ ,  $CH_3NH_2$ ,  $CH_3OH$ ,  $N_2H_4$ ,  $COCl_2$ , and  $H_2O_2$ . The subsequent low-temperature studies of single crystals of these volatile and unstable boranes were not without hazards. Vacuum line techniques were learned as we needed them. Fortunately, no serious injuries were incurred as a result of several explosions resulting from cracks in these vacuum systems. I was relieved, on one occasion, when I had taken Russell Grimes to a hospital in

Cambridge after one of these explosions to hear the doctor tell me, "Louis Fieser sends me much more interesting cases than you do." I still have in my office the air gun which I, or my young son, used on a number of occasions to destroy a cracked vacuum system from a safe distance. We also had chemical surprises, for example, when we found a presumed  $B_8$  hydride to be  $B_9H_{15}$  (16). Our only chemical analysis of this compound was the count of the numbers of boron and hydrogen atoms in the electron density map, which was calculated in those days from rough visual estimates of intensities of diffraction maxima on films.

### Three-Center Bonds Among Boron Atoms

At the fortunate time in 1953 of W. H. Eberhardt's sabbatical, he, Crawford, and I examined (17) the open boron hydrides  $B_2H_6$ ,  $B_4H_{10}$ ,  $B_5H_9$ ,  $B_5H_{11}$ , and  $B_{10}H_{14}$  from the viewpoint of three-center bonds; we also studied  $B_3H_9$ , the unknown polyhedral molecule  $B_4H_4$ , the then hypothetical ions  $B_6H_6^{2-}$  (Fig. 1) and  $B_{12}H_{12}^{2-}$  (Fig. 2) from the viewpoint of molecular orbitals. Longuet-Higgins and Roberts (18) also, independently, formed an early molecular orbital description almost like ours. One of the simple consequences of these studies was that electron-deficient molecules, defined as having more valence orbitals than electrons, are not really electron-deficient. I mean by this non sequitur that the three-center two-electron bonds make possible a simple description of these molecules and ions as species with filled orbitals. Filled molecular orbitals were later extended to closed polyhedral compounds  $B_nH_n$  for all values of  $n$  from 5 to 24, all of which have a formal charge of  $-2$ , even though hypothetical  $B_4H_4$  is neutral. In fact, all of the experimentally known ions, for  $6 \leq n \leq 12$ , do have  $-2$  charge. In addition to  $B_6H_6^{2-}$  (Fig. 1) and

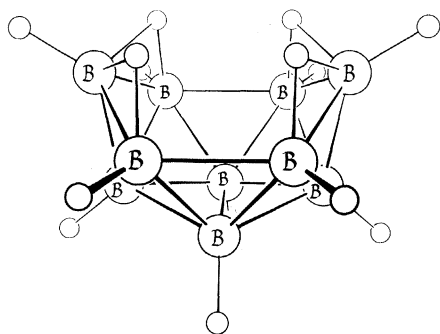


Fig. 4. Structure of  $B_{10}H_{14}$ .

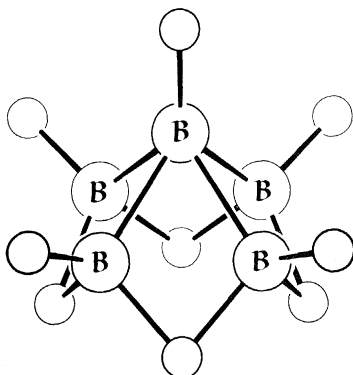


Fig. 5. Structure of  $B_5H_9$ .

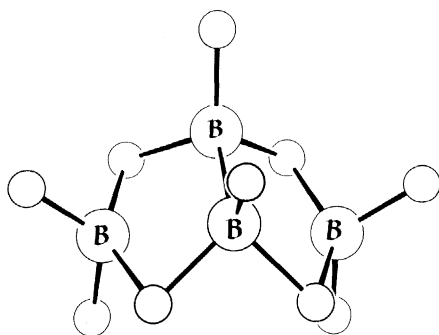


Fig. 6. Structure of  $B_4H_{10}$ .

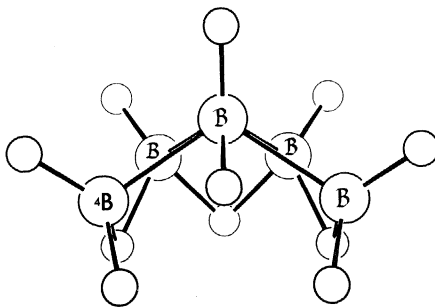


Fig. 7. Structure of  $B_5H_{11}$ .

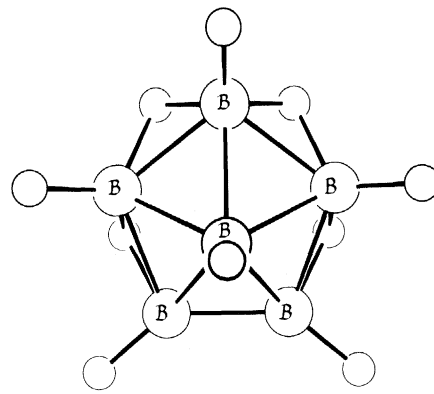


Fig. 8. Structure of  $B_6H_{10}$ .

$B_{12}H_{12}^{2-}$  (Fig. 2), those polyhedra for  $5 \leq n \leq 10$  are shown in Fig. 9. The isoelectronic series  $C_2B_{n-2}H_n$  is known for  $5 \leq n \leq 12$ .

Equations for the atom, orbital, and electron balance were formulated in our paper of 1954 (17), allowing prediction of many new chemical species. One simple form of these rules is exemplified for a neutral hydride formula  $B_pH_{p+q}$  in which each boron atom has at least one terminal hydrogen atom. If we define the number of BHB bridges as  $s$ , the number

of three-center BBB bonds as  $t$ , the number of two-center BB bonds as  $y$ , and the number of extra terminal hydrogens on each BH unit as  $x$ , then

$$\begin{aligned} s + x &= q \\ s + t &= p \\ p &= t + y + q/2 \end{aligned}$$

The first equation is the hydrogen balance. The second equation comes from the fact that each of the  $p$  boron atoms supplies four orbitals and only three electrons, and the extra orbital is utilized

in one of the two types of three-center bonds. Finally, if each BH unit is recognized as contributing a pair of electrons, these  $p$  pairs are used in BBB or BB bonds, or in half of the pairs required for the bridge and extra terminal hydrogens. These rules, and the accompanying valence structures, are especially helpful in describing those polyboron compounds which are open, but they are also useful for closed polyhedral molecules and ions.

There are two kinds of three-center

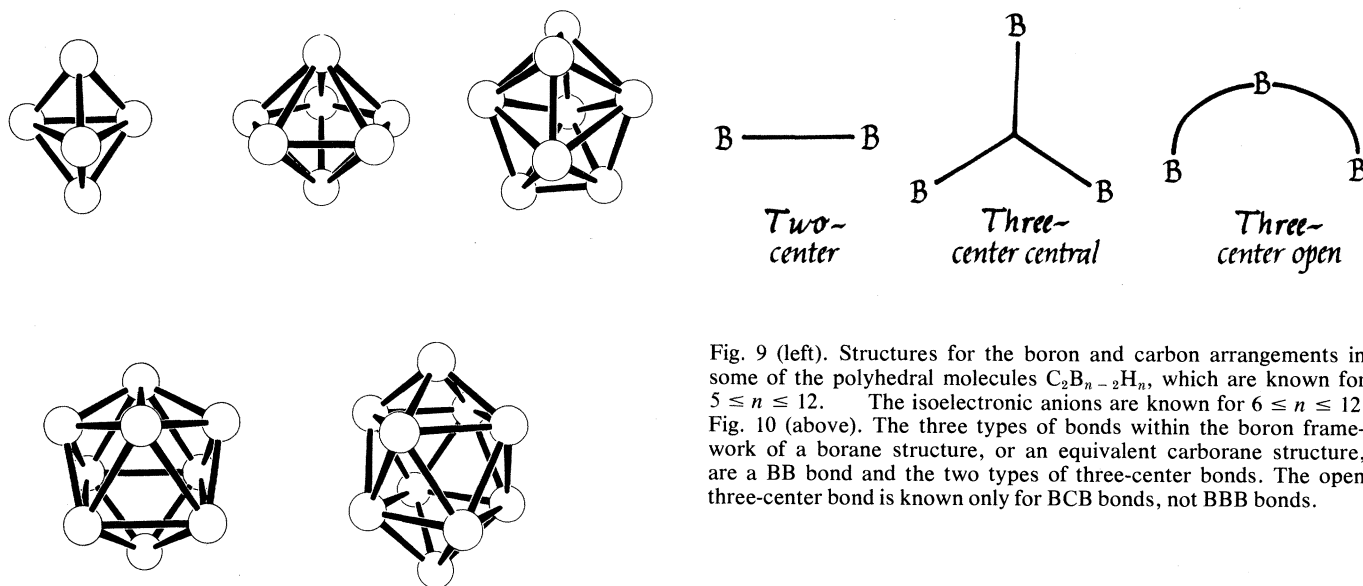


Fig. 9 (left). Structures for the boron and carbon arrangements in some of the polyhedral molecules  $C_2B_{n-2}H_n$ , which are known for  $5 \leq n \leq 12$ . The isoelectronic anions are known for  $6 \leq n \leq 12$ . Fig. 10 (above). The three types of bonds within the boron framework of a borane structure, or an equivalent carborane structure, are a BB bond and the two types of three-center bonds. The open three-center bond is known only for BCB bonds, not BBB bonds.

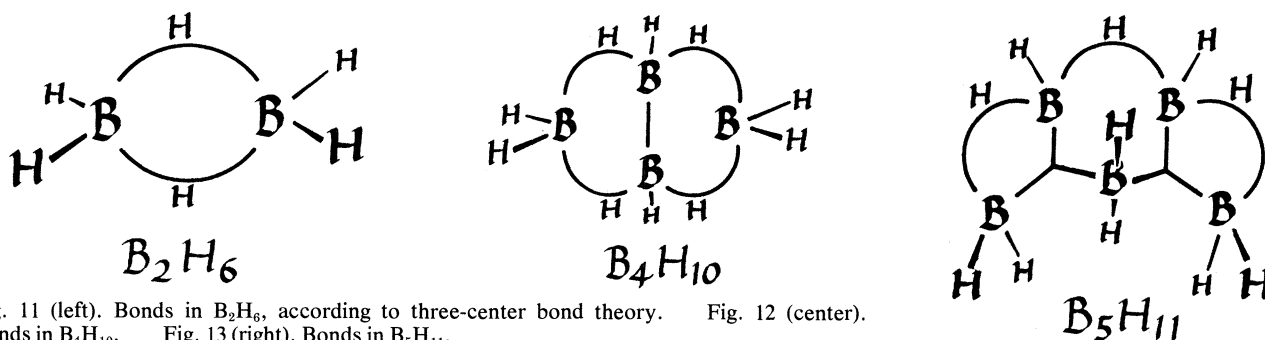


Fig. 11 (left). Bonds in  $B_2H_6$ , according to three-center bond theory. Fig. 12 (center). Bonds in  $B_4H_{10}$ . Fig. 13 (right). Bonds in  $B_5H_{11}$ .

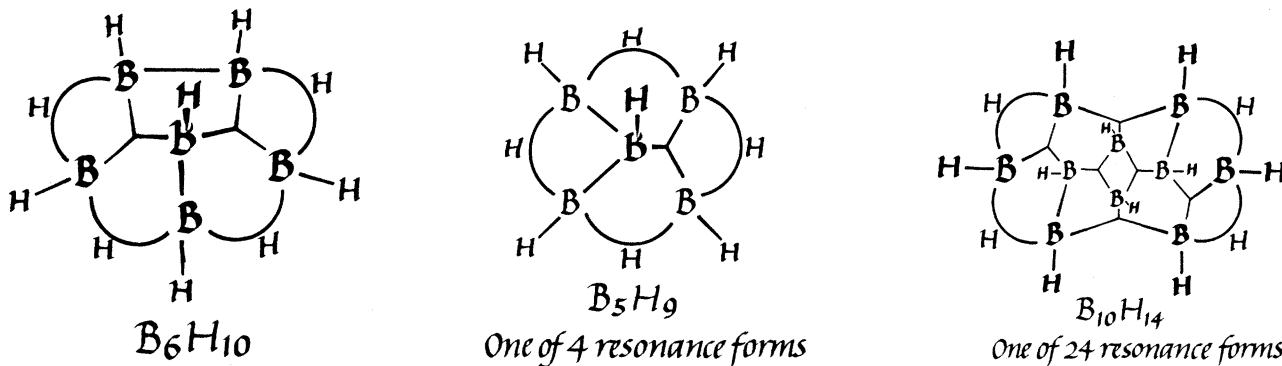


Fig. 14 (left). Bonds in  $B_6H_{10}$ . Fig. 15 (center). One of the four resonance structures for  $B_5H_9$ . The other three are obtained by reorientation of the framework bonds by  $90^\circ$  about the molecular fourfold axis. Fig. 16 (right). One of the 24 resonance structures for  $B_{10}H_{14}$ , omitting open three-center bonds.

bonds among three boron atoms (Fig. 10). The central three-center bond involves positive overlap among hybrid orbitals from each of three boron atoms; the open three-center bond involves, on the central atom, a  $\pi$  orbital which overlaps in a bonding manner with an orbital

from each of the adjacent boron atoms. The less compact  $B_2H_6$ ,  $B_4H_{10}$ ,  $B_5H_{11}$ , and  $B_6H_{10}$  structures (Figs. 11–14) are well described with the use of these three-center bonds, omitting open three-center BBB bonds for the moment. However,  $B_5H_9$  (Fig. 15) requires a reso-

nance hybrid of four valence structures, related by the fourfold symmetry; and  $B_{10}H_{14}$  (Fig. 16) requires a resonance hybrid of 24 valence structures.

Three-center bond theory was further developed in the next 22 years (19). I realized that the valence rules implied the existence of a large body of boron chemistry and then ventured predictions, some of which were actually verified experimentally. Dickerson and I (20) formalized my intuitive approach into a theory of connectivity of various bonding patterns within the three-center description. Also, geometrical constraints were introduced in order to avoid overcrowding of hydrogen atoms and to preserve known bonding angles about boron atoms among the boranes (21). More recently, Epstein and I (22) reformulated the topology, using central three-center BBB bonds, to the exclusion of open three-center BBB bonds. The recent work on localized molecular orbitals, which has led to the restriction of open three-center bonds, so far, to BCB bonds, is exemplified in a later part of this article.

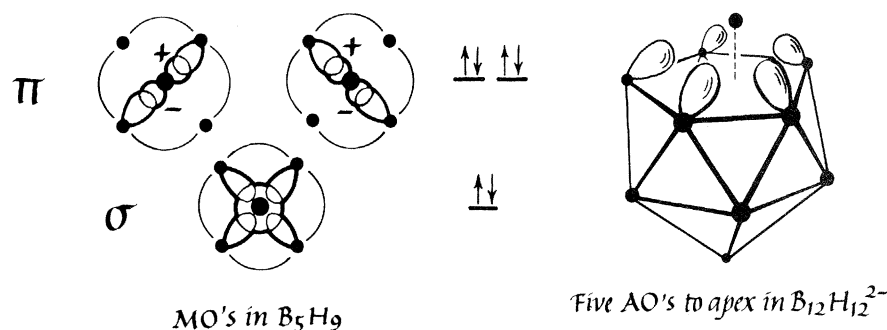


Fig. 17 (left). Symmetry molecular orbitals (MO's) in the boron framework of  $B_5H_9$ . The  $\sigma$  molecular orbital is a five-centered one, and each of the  $\pi$  components is actually an open three-center bond. Fig. 18 (right). A situation with five atomic orbitals (AO's) containing four electrons produced when a neutral BH unit is removed from the apex of  $B_{12}H_{12}^{2-}$  or  $C_5B_{10}H_{12}$ . These five atomic orbitals form a  $\sigma$  (bonding),  $\pi$  (bonding), and  $\delta$  (antibonding) set of five molecular orbitals, like those in the  $\pi$  electron system of  $C_5H_5$ .

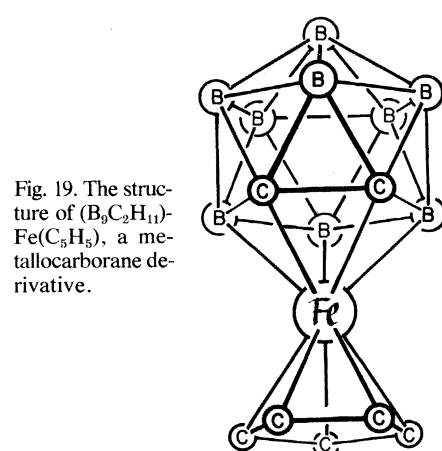


Fig. 19. The structure of  $(B_9C_2H_{11})-Fe(C_5H_5)$ , a metallocarborane derivative.

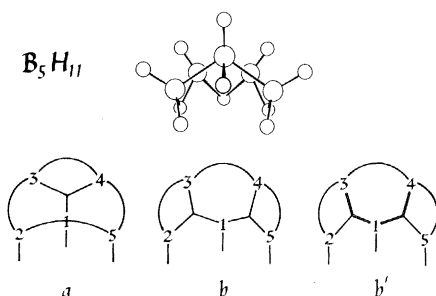


Fig. 20. Three valence structures of  $B_5H_{11}$  include (a) the disfavored open three-center bond, (b) the symmetrical central three-center bonds, and (b') the localized, slightly unsymmetrical three-center bonds. For clarity, one terminal BH bond has been omitted at each boron site in (a), (b), and (b').

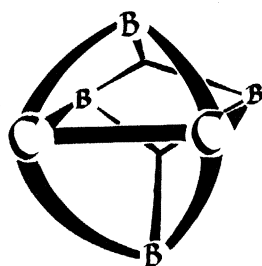
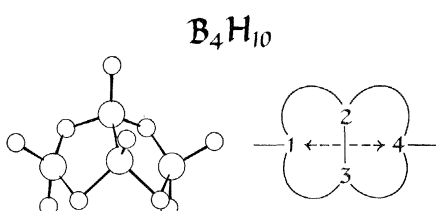
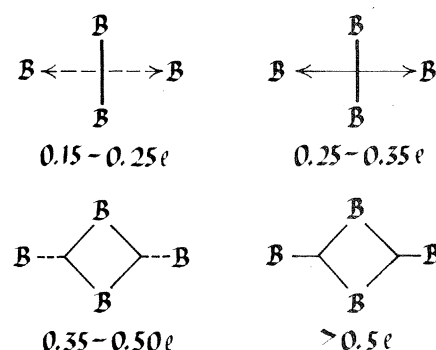


Fig. 21 (left). Localized molecular orbitals are shown in the framework of  $1,2-C_2B_4H_6$ . The open three-center bonds go through carbon. An external hydrogen has been omitted at each boron or carbon atom. Fig. 22 (top right). Notation is shown for amounts of single bond donation to adjacent boron atoms. Unsymmetrical donation may also occur. Fig. 23 (bottom right). Single bond donation in  $B_4H_{10}$  is about 0.19 e from the  $B_2B_3$  bond to each of the outer doubly bridged  $BH_2$  groups of the molecule.



## Molecular Orbital Studies of Boranes

Molecular orbitals are more appropriate for describing the valence structures of the polyhedral molecules and ions, and the more compact polyhedral fragments. Two simple examples will suffice. In  $B_5H_9$  there are three pairs of electrons in the boron framework, which has fourfold symmetry. The bonding is beautifully described, without resonance, by a simple  $\sigma$  and  $\pi$  set of molecular orbitals (17, 19, 23) (Fig. 17). These orbitals are similar to the bonding orbitals, for example, between planar fourfold cyclobutadiene ( $C_4H_4$ ) and a  $CH^+$  placed along the fourfold axis to give the carboonium ion  $C_5H_5^+$ .

A similar  $\sigma, \pi$  situation occurs (23) if a BH unit is removed from icosahedral  $B_{12}H_{12}^{2-}$ , leaving  $B_{11}H_{11}^{2-}$  having five atomic orbitals containing four electrons (Fig. 18). This set of five orbitals gives  $\sigma, \pi$  molecular orbitals which can bond to a similar set of  $\sigma, \pi$  orbitals from another atom or group of atoms supplying two more electrons. I suggested, conceptually, adding  $H_3^+$  to predict  $B_{11}H_{14}^-$ , for example. Although recognizing the similarity of this set of orbitals to those in  $C_5H_5$ , which was known to form ferrocene  $Fe(C_5H_5)_2$ , I did not then go quite so far as to suggest bonding of this  $B_{11}H_{11}^{2-}$  fragment to a transition metal. Later, Hawthorne did so, using these ideas as a starting point, and thereby created the

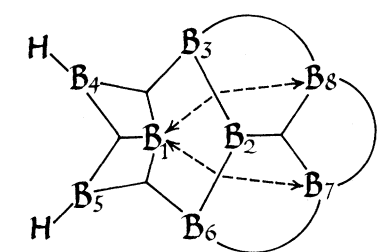
large family of metalloboranes and metallocarboranes (24) (Fig. 19).

In the early 1960's, when large-scale computing facilities became available to us, Roald Hoffmann and Lawrence Lohr independently programmed the extended Hückel method in my research group. Its first application was to boron chemistry (25), where, particularly in the carboranes (compounds of boron, carbon, and hydrogen), the charge distributions predicted sites of electrophilic and nucleophilic substitution. One of the rather simple rules which emerged was that nucleophilic attack occurs in a polyhedral carborane at a boron atom closest to carbon, whereas electrophilic attack was preferred at a boron farthest removed from carbon. Experimental studies of boranes and carboranes in which one or more hydrogens had been replaced by a halogen or by an amine group confirmed these predictions. The extended Hückel method became for a time the most widely used program for the study of molecular theory and reactions in complex organic and inorganic molecules. For example, the Woodward-Hoffmann rules, and related orbital concepts, were tested by their inventors (26) with the use of this theory.

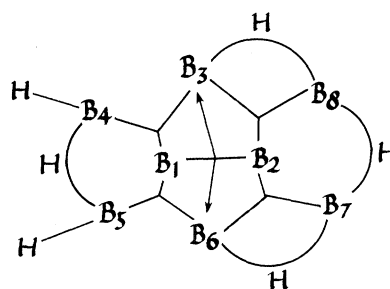
I thought then that progress in structure determination, for new polyborane species and for substituted boranes and carboranes, would be greatly accelerated if the  $^{11}\text{B}$  nuclear magnetic resonance spectra, rather than x-ray diffraction, could be used. One approach was empirical (27), whereas the other was purely theoretical. This latter approach required the development of a theory for fairly reliable calculation of chemical shifts of  $^{11}\text{B}$  from first principles of quantum mechanics (28). This theory, the coupled Hartree-Fock method for a molecule in a magnetic or electric field, yielded molecular constants good to a few to several percent (29) for many diatomic molecules. A striking result was the prediction of the paramagnetic nature of diatomic BH (30). However, the application of this method to the complex boranes still lies in the future, even after 13 years of effort. Although we understand some of the contributions to chemical shift and to diamagnetic and large temperature-independent paramagnetic effects, the use of this method for determination of the structure of complex polyboranes is still somewhat limited.

These programs yielded accurate self-consistent field molecular orbitals, which were explored in other areas of chemistry, as well as in the boranes and carboranes. One example was the first accu-

rate calculation of the barrier to internal rotation in ethane (31). At this point, my research students and I set out to explore the gap between extended Hückel theory and self-consistent field theory. We achieved by stages (32) a molecular orbital theory (33), still being extended, which was applicable to large polyboranes and other molecules and which had essentially the accuracy of self-consistent field methods. Molecular orbital methods which do not go beyond symmetry orbitals tend to make each molecule a separate case. Hence, we began only a few years ago to explore the connections between these symmetry orbitals and the three-center bonds discussed in the earlier section.



$\text{B}_8\text{H}_{13}^-$



$\text{B}_8\text{H}_{14}$

## Localized Molecular Orbitals

Ordinarily, molecular orbitals are classified according to their symmetry types. However, it is possible to make linear combinations of molecular orbitals of different symmetries in such a way that the total electron density of the molecule remains invariant. The most popular methods are those of Edmiston and Ruedenberg (34) who maximize

$$\sum_i \iint \phi_i(1) \phi_i(1) \frac{1}{r_{12}} \phi_i(2) \phi_i(2) dV_1 dV_2$$

and of Boys (35) who minimizes

$$\sum_i \iint \phi_i(1) \phi_i(1) r_{12}^2 \phi_i(2) \phi_i(2) dV_1 dV_2$$

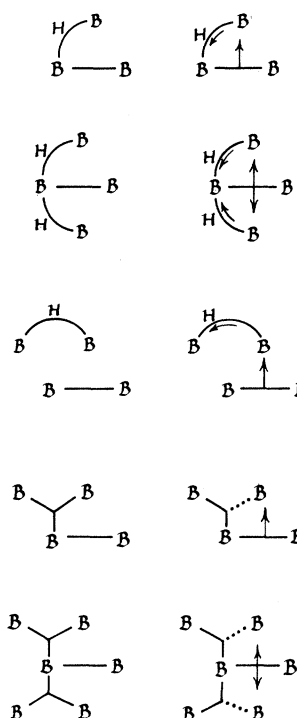
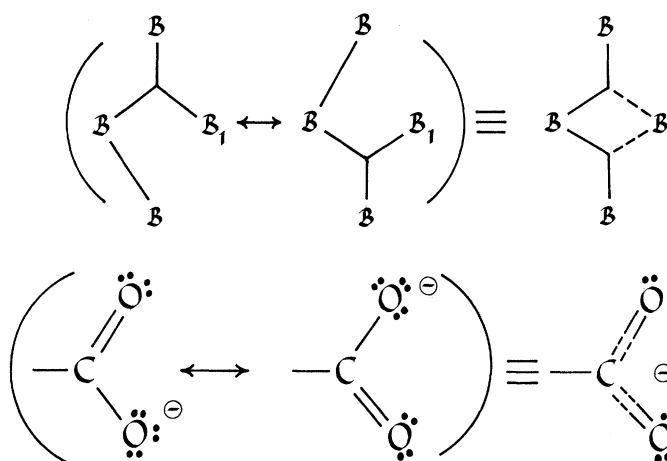


Fig. 24 (top left). Single bond donation is shown in  $\text{B}_8\text{H}_{13}^-$ . Fig. 25 (bottom left). Donation occurs from the  $\text{B}_1\text{B}_2$  single bond in  $\text{B}_8\text{H}_{14}$ . Fig. 26 (right). Some common patterns of single bond donation cause hydrogen atom displacement and electron withdrawal from the atom to which donation occurs.

Fig. 27 (top). Equivalence is shown of the two fractional three-center bonds to a resonance hybrid of a single bond and a three-center bond. Fig. 28 (bottom). The four localized molecular orbitals in the carboxylate anion have a charge distribution which shows displacement toward oxygen. The equivalent resonance hybrid is given at the left.



Here,  $\phi_i$  is the  $i$ th molecular orbital,  $r_{12}$  is the interelectronic distance, and  $dV_1$  is the element of volume for electron 1. These procedures, respectively, maxi-

mize the repulsions of those electron pairs within each molecular orbital and minimize the orbital self-extension of each electron pair. Thus, in a slightly dif-

ferent manner, the symmetry orbitals are converted into linear combinations which are a good approximation to the localized electron-pair bond. These ob-

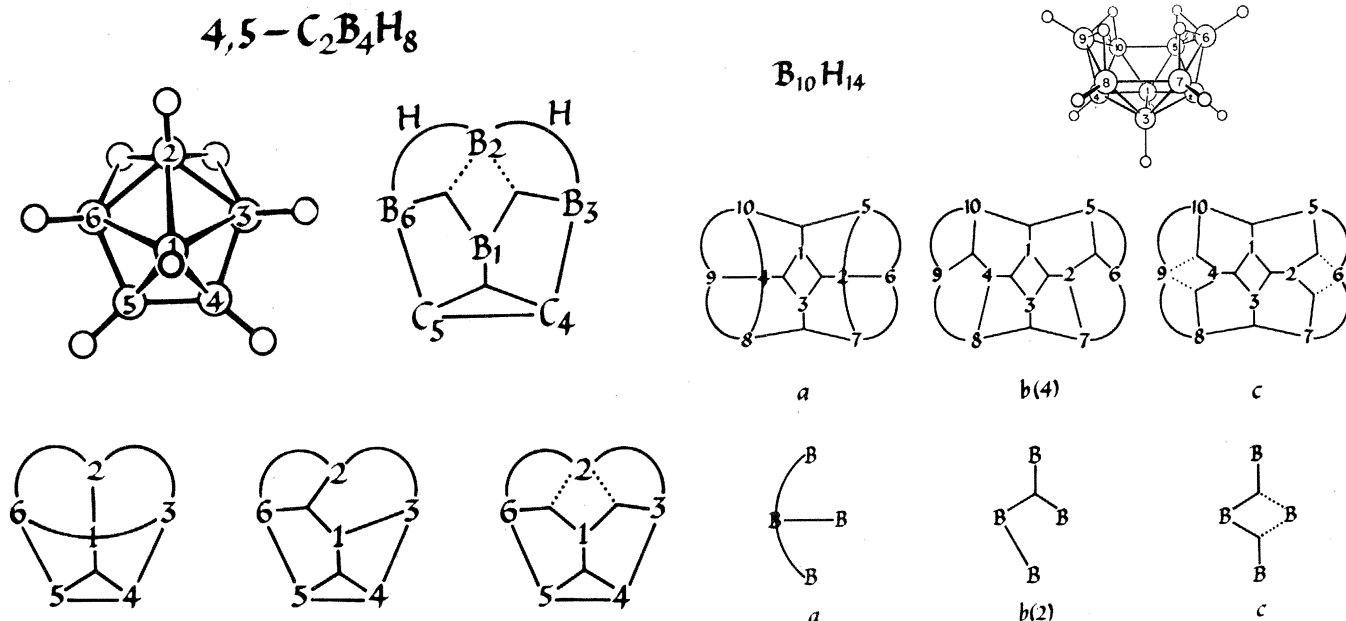


Fig. 29 (left). Localized orbitals in 4,5- $C_2B_4H_8$  show fractional donation to atom  $B_2$  as dotted lines. Fig. 30 (right). The pattern of fractional bonds, dotted toward  $B_6$  and  $B_9$  in  $B_{10}H_{14}$  can be expected when there is resonance of the type shown in the central diagram, or when one is tempted to draw open three-center BBB bonds as shown on the left. The fractional bond description is preferred.

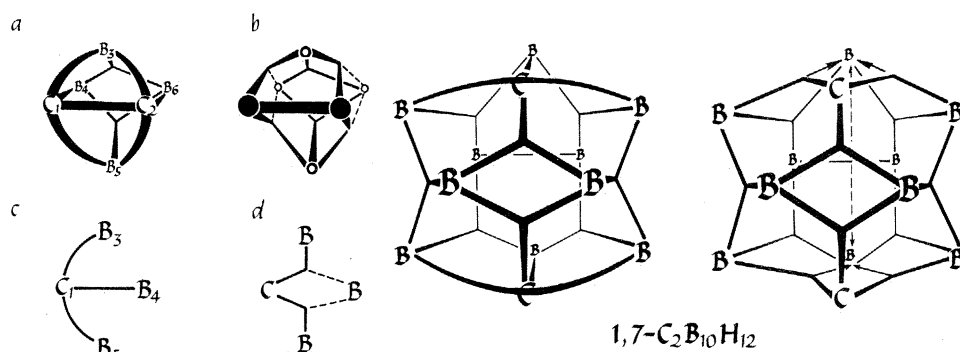


Fig. 31 (left). In 1,2- $C_2B_4H_6$  the Edmiston-Ruedenberg localization yields open three-center bonds at carbon, whereas the Boys localization gives fractional three-center bonds. The latter procedure gives greater emphasis to the separation of orbital centroids when they are on the same atom. Fig. 32 (right). A situation parallel to that of Fig. 31 may occur in 1,7- $C_2B_{10}H_{12}$ , where the Boys localization (right) shows fractional bonds. The open three-center bond description may be found by the Edmiston-Ruedenberg procedure, if and when the calculations can be made.

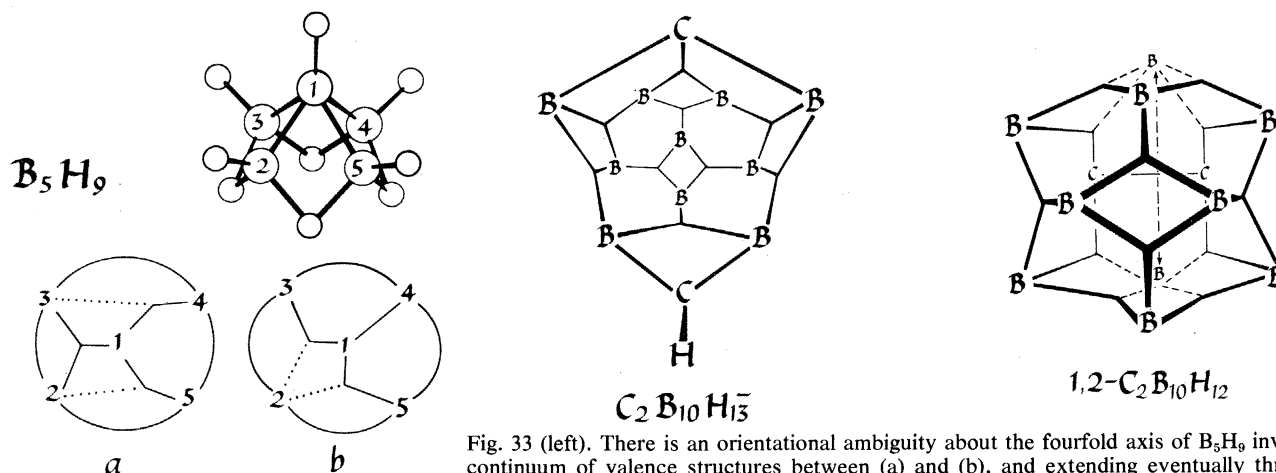


Fig. 33 (left). There is an orientational ambiguity about the fourfold axis of  $B_5H_9$  involving a continuum of valence structures between (a) and (b), and extending eventually throughout the complete  $360^\circ$  range. Fig. 34 (center). There is little fractional bonding in the localized orbitals of the nearly polyhedral  $C_2B_{10}H_{13}^-$  ion. Fig. 35 (right). The localized orbitals obtained from 1,2- $C_2B_{10}H_{12}$  by the Boys procedure are the same as those found in 1,7- $C_2B_{10}H_{12}$  in spite of the differences in the positions of carbon atoms relative to boron atoms.

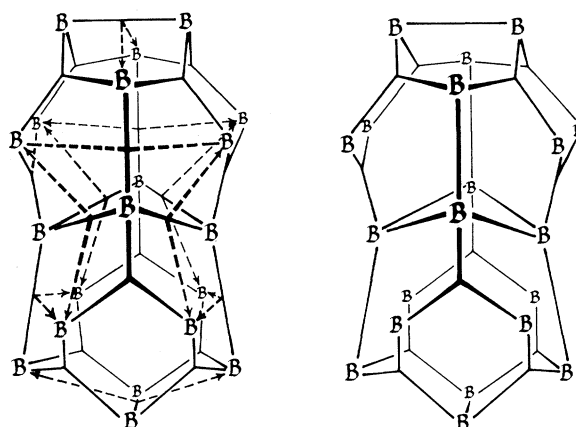
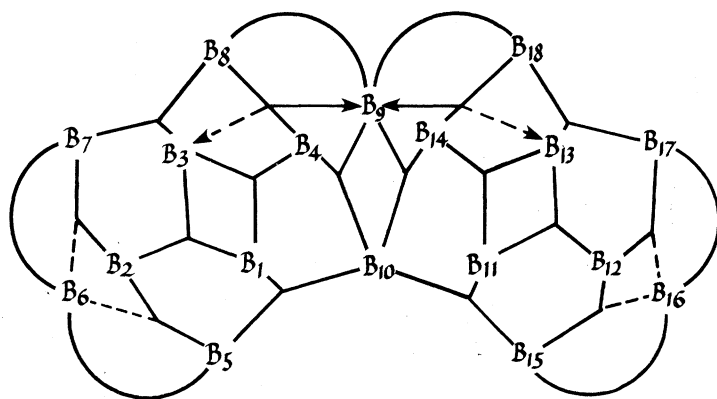
jective procedures, without adjustable parameters, have been compared in some detail (36). They provide support of three-center bond descriptions within a theoretical chemical framework. Also, they test the level at which two-center and three-center bonds require some further delocalization. These studies have also provided preferred descriptions of valence structures, often eliminating or reducing the need for resonance hybrids.

Open three-center and central three-center BBB bonds are almost equivalent descriptions. If both types are included, there are 111 resonance structures for  $B_{10}H_{14}$ , of which 24 are based only on central three-center bonds. In  $B_5H_{11}$  (Fig. 20) two slightly unsymmetrical central three-center BBB bonds are found (37) by both localization procedures (Fig. 20b'), whereas the open three-center description is not favored. In a series of studies of localized molecular orbitals

in all of the boron hydrides, carboranes, and ions of known geometry, we have never found an open three-center BBB bond. However, open three-center BCB bonds do exist. For example, the open three-center BCB bond (38) occurs twice in  $1,2-C_2B_4H_6$  (Fig. 21), when the Edmiston-Ruedenberg procedure is used. A comparison of these results with those of the Boys procedure is given below. In the simplest molecular orbital description of an open three-center bond, the electron pair is distributed as  $e/2$ ,  $e$ ,  $e/2$  among these three atoms. It is probable that the extra nuclear charge of carbon stabilizes this distribution, to give open three-center bonds rather than nearly equivalent central three-center bonds, when carbon is the middle atom.

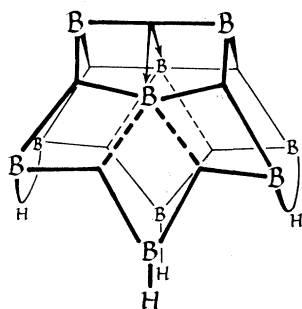
Another new general result is that almost every single bond within a triangulated borane or carborane framework shows some donation to the near-

est adjacent atoms (Fig. 22). This tendency for multicentered bonding usually involves 10 percent or less of the electron pair. In  $B_4H_{10}$ , about 0.2  $e$  is donated (37) from the single BB bond to each of atoms  $B_1$  and  $B_4$ , which themselves are relatively electron-deficient because of the open three-center bonds of the hydrogen bridges (Fig. 23). This donation then causes these hydrogen bridges to become unsymmetrical, displaced toward  $B_2$  and  $B_3$ , in accord with the results obtained from our x-ray diffraction study. More generally, this donation causes electron withdrawal along other bonds in the molecule, whether or not hydrogen bridges are available for accommodating this electron displacement. Two additional examples are illustrated in  $B_8H_{13}^-$  and in the predicted structure of  $B_8H_{14}$ , respectively (39) (Figs. 24 and 25). I have abstracted from these examples some typical modes of

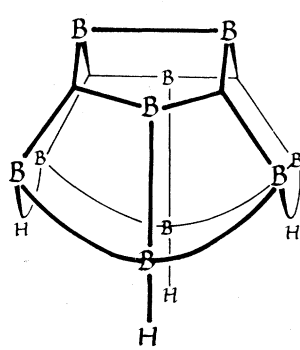


$B_{20}H_{16}$

Fig. 36 (left). Single bond donation and fractional bonds occur in iso- $B_{18}H_{22}$ , a molecule having a twofold axis only, and no terminal hydrogen atoms on  $B_9$  and  $B_{10}$ . Fig. 37 (right). Donation and nondonation localized orbitals are shown for  $B_{20}H_{16}$ , in which the four borons nearest the equatorial belt have no terminal hydrogens. Boron atoms  $B_9$  through  $B_{16}$  inclusive are particularly electron-deficient, and receive substantial donation from single bonds. These eight boron atoms have only two framework bonds in the figure at the right.

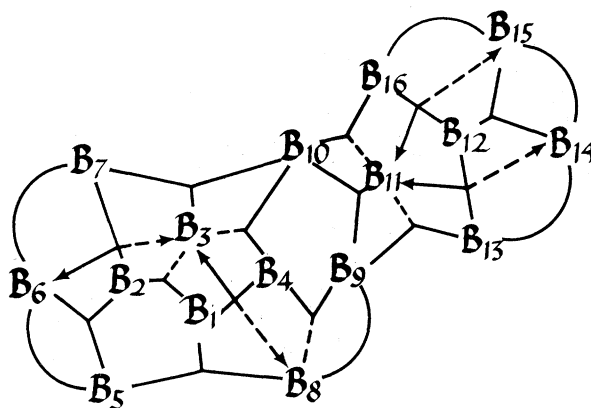


$B_{10}H_{14}^{2-}(\text{LMO's})$



$B_{10}H_{14}^{2-}(\text{open})$

Fig. 38 (above). A relationship similar to that in  $B_{20}H_{16}$  occurs in  $B_{10}H_{14}^{2-}$ . The preferred localized molecular orbital (LMO) structure is shown on the left; the open three-center bond structure without donation (right) is an oversimplified valence structure.



$B_{16}H_{20}$

Fig. 39 (right). A rather complex pattern of localized molecular orbitals is shown for  $B_{16}H_{20}$ . Bond donations can be withdrawn by the reader in order to discover the preferred valence bond structures of the simpler theory. This single valence structure replaces a resonance hybrid of 216 valence structures based upon central three-center bonds and single bonds. Atoms  $B_9$  and  $B_{10}$  do not have terminal hydrogens.

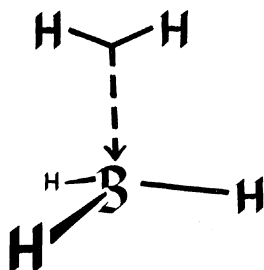


Fig. 40. Fractional donation of a single bond between two hydrogen atoms to the vacant orbital of a slightly pyramidal, nearly planar,  $\text{BH}_3$  group. The resulting  $\text{BH}_5$  molecule is a very short-lived reaction intermediate.

single bond donation, and accompanying electron withdrawal or hydrogen displacement, in Fig. 26. These and similar valence diagrams may be useful in understanding intramolecular distortions and reaction mechanisms.

A new type of bonding, which is conceptually transferable among these molecules, is described as fractional three-center bonds (40). Its simplest interpretation is the replacement of a pair of resonance structures by a single valence structure (Fig. 27). The fractional use of orbitals, indicated by dashed lines, increases the apparent number of bonds to a given boron above the usual four, in an element in the first row of the periodic table. However, the Pauli exclusion principle is not violated because less than a full atomic orbital is required at a fractional bond. Indeed, the localized molecular orbitals are themselves derived from wave functions for which the exclusion principle is rigorously introduced. The use of fractional bonds to reduce the number of resonance hybrids, often to a single preferred structure, is not limited to boranes and their relatives. Our rather extensive studies of bonding among atoms other than boron have indicated that these simplified localized molecular orbitals may be an informative and useful alternative to the more conventional valence bond and molecular orbital descriptions in other parts of the periodic table. A very simple example, the carboxylate anion (41), is shown in Fig. 28.

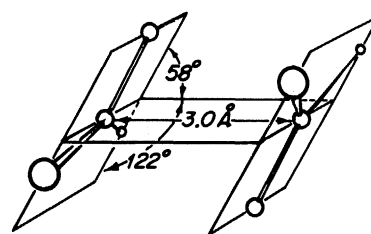
Fractional bonds to atom  $\text{B}_2$  in 4,5- $\text{C}_2\text{B}_4\text{H}_8$  are preferred (42) over a resonance hybrid of a single and a central three-center bond, and also are preferred over the open three-center bond (Fig. 29). Also, the bonding of the two carbon atoms in this carborane by both a single bond and a central three-center bond has not been found in boranes and, in particular, does not occur in  $\text{B}_6\text{H}_{10}$ , which is isoelectronic with 4,5- $\text{C}_2\text{B}_4\text{H}_8$ . Fractional bonds give a particularly simple valence description (39) of bonding in

$\text{B}_{10}\text{H}_{14}$  (Fig. 30), where the single valence structure (Fig. 30c) replaces a resonance hybrid of 24 central three-center bond structures. A very similar simplification (39) occurs in  $\text{B}_{10}\text{H}_{14}^{2-}$ , where the two pairs of fractional bonds are dotted toward atoms  $\text{B}_2$  and  $\text{B}_4$ , rather than toward  $\text{B}_6$  and  $\text{B}_8$ .

Similar pairs of fractional bonds are found by Boys's localization procedure in the polyhedral carboranes 1,2- $\text{C}_2\text{B}_4\text{H}_6$  (Fig. 31) and 1,7- $\text{C}_2\text{B}_{10}\text{H}_{12}$  (Fig. 32). Perhaps this procedure tends to exaggerate the separation of charge centroids of bonds when they lie at or near a single center. For this reason, we tend to prefer (36) the almost equivalent open three-center bonds, as found by the Edmiston-Ruedenberg procedure in 1,2- $\text{C}_2\text{B}_4\text{H}_6$ . When it becomes economically feasible to test this alternative in 1,7- $\text{C}_2\text{B}_{10}\text{H}_{12}$ , I would guess that localized, open three-center bonds will be found, centered at carbon atoms, in this molecule, like those in 1,2- $\text{C}_2\text{B}_4\text{H}_6$ .

Fractional three-center bonds are not always unique, particularly in aromatic hydrocarbons or in those boranes that have a valence pattern similar to that in the aromatics. An example of this orientational ambiguity occurs in the boron framework bonds in  $\text{B}_5\text{H}_9$  (Fig. 33). Actually, the two valence structures represent extremes over a  $45^\circ$  range of orientation angle, about the fourfold axis. There is a continuum of valence structures between these extremes. Moreover, this ambiguity continues throughout the whole  $360^\circ$ , in accord with the fourfold symmetry which the electron density must have in this molecule. All of these valence structures are equally preferred, and each has a total electron density consistent with the fourfold molecular symmetry.

In more complex molecules one can find various degrees of simplicity in the bonding patterns of localized molecular orbitals. In  $\text{C}_2\text{B}_{10}\text{H}_{13}^-$ , which has a somewhat open near-icosahedral  $\text{C}_2\text{B}_{10}$  arrangement, the bonding is especially simple (43), not requiring resonance or appreciable fractional bonding (Fig. 34). In 1,2- $\text{C}_2\text{B}_{10}\text{H}_{12}$ , another simple idea occurs: the bonding, as found by Boys's procedure, is to a good approximation just like that in 1,7- $\text{C}_2\text{B}_{10}\text{H}_{12}$  in spite of the very different positions of the two carbon atoms relative to each other and to their boron neighbors (Fig. 35). Thus there is some tendency for bonding invariance in closely related geometrical structures. In iso- $\text{B}_{18}\text{H}_{22}$ , we find (44) both single bond donation, from  $\text{B}_3\text{B}_8$  and  $\text{B}_{14}\text{H}_{18}$ , and fractional bonds, to  $\text{B}_6$  and  $\text{B}_{16}$  (Fig. 36). Here, the single bond



### Symmetry $C_{2h}$

Fig. 41. Approximate geometry of the transition state when two  $\text{BH}_3$  molecules form  $\text{B}_2\text{H}_6$ . This geometry is favored over that in an unsymmetrical approach of two  $\text{BH}_3$  molecules.

donations are greater toward  $\text{B}_9$ , which is relatively electron-deficient, than toward  $\text{B}_3$  and  $\text{B}_{13}$ . In  $\text{B}_{20}\text{H}_{16}$  there is a remarkable amount of single-bond donation, particularly toward the electron-deficient atoms  $\text{B}_9$  through  $\text{B}_{16}$  inclusive (Fig. 37), and the valence structure of each half is clearly like that in  $\text{B}_{10}\text{H}_{14}^{2-}$  (Fig. 38) rather than like that in  $\text{B}_{10}\text{H}_{14}$  (Fig. 30).

The rather complex localized molecular orbitals in  $\text{B}_{16}\text{H}_{20}$  (Fig. 39) are dominated by the three-center bond approximation; in addition, they are modified by single bond donation accompanied by electron withdrawal from atoms to which donation occurs (44). With recognition that atoms  $\text{B}_9$  and  $\text{B}_{10}$  have no terminal hydrogens attached to them, I offer the reader a challenge to find the close relative valence structures which do not have fractional bonding or single bond donation in this molecule.

Finally, the bonding in reaction intermediates is a new area of study, primarily by purely theoretical methods. In  $\text{BH}_3$  (Fig. 40) there is only a very weak donor bond from  $\text{H}_2$  to the vacant orbital of  $\text{BH}_3$  (45). This weakness is probably due to the absence of a pathway for back-donation. On the other hand, in the dimerization of two  $\text{BH}_3$  molecules to form  $\text{B}_2\text{H}_6$ , donation of electron density from one terminal hydrogen to the boron atom of the other  $\text{BH}_3$  group is balanced by a symmetrically related donation toward the first  $\text{BH}_3$  group (46) (Fig. 41). Our other recent progress in theoretical studies of bonding in reaction intermediates, such as  $\text{B}_3\text{H}_7$  and  $\text{B}_4\text{H}_8$ , shows that the more stable transient species may have a vacant orbital (47) on one boron atom, because of the strain involved when that vacant orbital is filled by the conversion of a terminal  $\text{BH}$  bond to a bridge  $\text{BHB}$  bond. Actually less is known of the detailed reaction mechanism for reactions of boranes and their related compounds than for organic reactions of comparable



complexity. Surely, this is a fruitful area for future research.

I shall stop here, omitting descriptions of bonding in large polyhedral borane anions and other related compounds. Also, polyhedral rearrangements, hydrogen atom tautomerism, and particularly the use of bonding theory in bringing some degree of order to chemical transformations of the boranes have been omitted. Attention has thus been concentrated on those aspects of chemical bonding which have been especially illuminated by the molecular and crystal structures that we and others have studied over these many years.

#### References and Notes

1. A. Stock, *Hydrides of Boron and Silicon* (Cornell Univ. Press, Ithaca, N.Y., 1933).
2. N. V. Sidgwick, *The Chemical Elements and Their Compounds* (Clarendon, London, 1950), p. 338.
3. L. Pauling, *The Nature of the Chemical Bond* (Cornell Univ. Press, Ithaca, N.Y., 1940).
4. F. Stitt, *J. Chem. Phys.* **8**, 981 (1940); *ibid.* **9**, 780 (1941).
5. H. C. Longuet-Higgins and R. P. Bell, *J. Chem. Soc.* **1943**, 250 (1943); K. S. Pitzer, *J. Am. Chem. Soc.* **67**, 1126 (1945); R. S. Mulliken, *Chem. Rev.* **41**, 207 (1947).
6. H. C. Longuet-Higgins, *J. Chim. Phys.* **46**, 268 (1949).
7. W. C. Price, *J. Chem. Phys.* **15**, 614 (1947); *ibid.* **16**, 894 (1948).
8. J. S. Kasper, C. M. Lucht, D. Harker, *Acta Crystallogr.* **3**, 436 (1950).
9. W. J. Dulmage and W. N. Lipscomb, *J. Am. Chem. Soc.* **73**, 3539 (1951); *Acta Crystallogr.* **5**, 260 (1952); K. Hedberg, M. E. Jones, V. Schomaker, *J. Am. Chem. Soc.* **73**, 3538 (1951); *Proc. Natl. Acad. Sci. U.S.A.* **38**, 679 (1952).
10. C. E. Nordman and W. N. Lipscomb, *J. Am. Chem. Soc.* **75**, 4116 (1953); *J. Chem. Phys.* **21**, 1856 (1953); M. E. Jones, K. Hedberg, V. Schomaker, *J. Am. Chem. Soc.* **75**, 4116 (1953).
11. L. Lavine and W. N. Lipscomb, *J. Chem. Phys.* **22**, 614 (1954).
12. M. Atoji and W. N. Lipscomb, *ibid.* **21**, 172 (1953); *Acta Crystallogr.* **6**, 547 (1953).
13. K. Eriks, W. N. Lipscomb, R. Schaeffer, *J. Chem. Phys.* **22**, 754 (1954); F. L. Hirshfeld, K. Eriks, R. E. Dickerson, E. L. Lippert, Jr., W. N. Lipscomb, *ibid.* **28**, 56 (1958).
14. S. C. Abrahams, R. L. Collin, W. N. Lipscomb, T. B. Reed, *Rev. Sci. Instrum.* **21**, 396 (1950).
15. H. S. Kauffman and I. Fankuchen, *ibid.* **20**, 733 (1949).
16. R. E. Dickerson, P. J. Wheatley, P. A. Howell, W. N. Lipscomb, *J. Chem. Phys.* **27**, 200 (1957).
17. W. H. Eberhardt, B. Crawford, Jr., W. N. Lipscomb, *ibid.* **22**, 989 (1954).
18. H. C. Longuet-Higgins and M. de V. Roberts, *Proc. R. Soc. London Ser. A* **224**, 336 (1954); *ibid.* **230**, 110 (1955).
19. W. N. Lipscomb, *Boron Hydrides* (Benjamin, New York, 1963).
20. R. E. Dickerson and W. N. Lipscomb, *J. Chem. Phys.* **27**, 212 (1957).
21. W. N. Lipscomb, *Inorg. Chem.* **3**, 1683 (1964).
22. I. R. Epstein and W. N. Lipscomb, *ibid.* **10**, 1921 (1971).
23. E. B. Moore, Jr., L. L. Lohr, Jr., W. N. Lipscomb, *J. Chem. Phys.* **35**, 1329 (1961).
24. M. F. Hawthorne, *Acc. Chem. Res.* **1**, 281 (1968).
25. R. Hoffmann and W. N. Lipscomb, *J. Chem. Phys.* **37**, 2872 (1962); *ibid.* **36**, 2179 (1962); *ibid.*, p. 3489.
26. R. B. Woodward and R. Hoffmann, *The Conservation of Orbital Symmetry* (Verlag Chemie, Weinheim, Germany, 1970).
27. G. R. Eaton and W. N. Lipscomb, *NMR Studies of Boron Hydrides and Related Compounds* (Benjamin, New York, 1969).
28. R. M. Stevens, R. M. Pitzer, W. N. Lipscomb, *J. Chem. Phys.* **38**, 550 (1963).
29. W. N. Lipscomb, in *MTP [Medical and Technical Publishing Co. Ltd.] International Review of Science, Theoretical Chemistry. Physical Chemistry, Series One*, A. D. Buckingham and W. Byers Brown, Eds. (Butterworths, London, 1972), vol. 1, pp. 167-196.
30. R. A. Hegstrom and W. N. Lipscomb, *Rev. Mod. Phys.* **40**, 354 (1968).
31. R. M. Pitzer and W. N. Lipscomb, *J. Chem. Phys.* **39**, 1995 (1963).
32. M. D. Newton, F. P. Boer, W. N. Lipscomb, *J. Am. Chem. Soc.* **88**, 2353 (1966); F. P. Boer, M. D. Newton, W. N. Lipscomb, *ibid.*, p. 2361.
33. T. A. Halgren and W. N. Lipscomb, *Proc. Natl. Acad. Sci. U.S.A.* **69**, 652 (1972); *J. Chem. Phys.* **58**, 1569 (1973).
34. C. Edmiston and K. Ruedenberg, *Rev. Mod. Phys.* **35**, 457 (1963).
35. S. F. Boys, in *Quantum Theory of Atoms, Molecules and the Solid State*, P. O. Löwdin, Ed. (Academic Press, New York, 1966), pp. 253-262.
36. D. A. Kleier, T. A. Halgren, J. H. Hall, Jr., W. N. Lipscomb, *J. Chem. Phys.* **61**, 3905 (1974).
37. E. Switkes, W. N. Lipscomb, M. D. Newton, *J. Am. Chem. Soc.* **92**, 3847 (1970).
38. I. R. Epstein, D. S. Marynick, W. N. Lipscomb, *ibid.* **95**, 1760 (1973).
39. J. H. Hall, Jr., D. A. Dixon, D. A. Kleier, T. A. Halgren, L. D. Brown, W. N. Lipscomb, *ibid.* **97**, 4202 (1975).
40. D. S. Marynick and W. N. Lipscomb, *ibid.* **94**, 8692 (1972).
41. D. A. Dixon and W. N. Lipscomb, *J. Biol. Chem.* **251**, 5992 (1976).
42. D. S. Marynick and W. N. Lipscomb, *J. Am. Chem. Soc.* **94**, 8699 (1972).
43. E. I. Tolpin and W. N. Lipscomb, *Inorg. Chem.* **12**, 2257 (1973).
44. D. A. Dixon, D. A. Kleier, T. A. Halgren, W. N. Lipscomb, *J. Am. Chem. Soc.* **98**, 2086 (1976).
45. M. M. Kreevoy and J. E. C. Hutchins, *ibid.* **94**, 6371 (1972); I. M. Pepperberg, T. A. Halgren, W. N. Lipscomb, *ibid.* **98**, 3442 (1976); C. Hoheisel and W. Kutzelnigg, *ibid.* **97**, 6970 (1975); J. B. Collins, P. v. R. Schleyer, J. S. Binkley, J. A. Pople, L. Radom, *ibid.*, in press; P. C. Hariharan, W. A. Latham, J. A. Pople, *Chem. Phys. Lett.* **14**, 385 (1972).
46. D. A. Dixon, I. M. Pepperberg, W. N. Lipscomb, *J. Am. Chem. Soc.* **96**, 1325 (1974).
47. J. A. Dupont and R. Schaeffer, *J. Inorg. Nucl. Chem.* **15**, 310 (1960).
48. It remains to give credit where it really belongs, to my research associates: graduate students, undergraduates, postdoctoral fellows, and other colleagues who have coauthored nearly all of these studies. For the figures of this manuscript, and of the lecture, I thank Jean Evans. I am most grateful to the Office of Naval Research which supported this research during the period from 1948 to 1976, a remarkably long time. I am most aware of the great influence of Linus Pauling on my whole scientific career. Finally, this manuscript is dedicated to the memory of my sister, Helen Porter Lipscomb, composer, teacher, and performer.

## A Response Regulator Model in a Simple Sensory System

Bacterial behavior can provide insight into the molecular aspects of more complex behavioral systems.

D. E. Koshland, Jr.

A modern molecular biologist might paraphrase the poet Pope by saying, "The proper study of mankind is the bacterium." Similarities in metabolic pathways, adenosine triphosphate as a central energy source, and the genetic code which transcend species suggest that there are universal biological principles.

The word "behavior" on the other hand is usually used to describe phenomena in higher differentiated species, and words like judgment, memory, choice, and discrimination seem inappropriate when applied to organisms at the lower end of the phylogenetic tree. Yet biologists have recognized that the study of behavior

applies even to the simplest species (1, 2). Hence, the molecular mechanisms involved in bacterial behavior may provide insight into the behavior of more complex organisms.

Sensory and neural processes are in a sense the ultimate regulatory mechanism, the refinement of "feedback" and "feedforward" information-processing to the most advanced level. It seems of interest, therefore, to examine sensory systems, to determine, on the one hand, if known processes are utilized to provide their regulation and, on the other, if any new principles or new combinations of principles are revealed. In this article, the behavioral response of bacteria is analyzed in terms of a response regulator model which may be useful in explaining regulation and behavior in more complex organisms.

The author is professor of biochemistry at the University of California, Berkeley 94720. This article is adapted from the text of the Earl A. Sutherland Memorial Lecture, delivered by the author at the University of Miami, Miami, Florida.